

Letters to the Editor

Some Comments Concerning the Discrete Eigenvalue

I. INTRODUCTION

As alternatives to the “exact” expression given in Ref. 1 for the discrete eigenvalue defined (for the simplest of all non-trivial problems in transport theory) as the positive zero of

$$\Lambda(z) = 1 + \frac{cz}{2} \int_{-1}^1 \frac{d\mu}{\mu - z}, \quad (1)$$

we report (again) the two “exact” expressions reported in Refs. 2 and 3:

$$\nu_0 = (1 - c)^{-1/2} \exp \left\{ -\frac{1}{\pi} \int_0^1 \Theta(c, x) \frac{dx}{x} \right\} \quad (2a)$$

and

$$\nu_0 = \left\{ \frac{3 - 2c}{3 - 3c} - \frac{2}{\pi} \int_0^1 x \Theta(c, x) dx \right\}^{1/2} \quad (2b)$$

where, using *continuous* values on $[0, \pi]$ of the arctan function, we write

$$\Theta(c, x) = \arctan \left\{ \frac{c\pi x}{2[1 - cx \operatorname{arctanh}(x)]} \right\}. \quad (3)$$

II. RESULTS

We have found, using the Maple V (release 4) software package and the three lines of code given in Sec. III, that we can evaluate Eqs. (2) for various cases of $c \in [0.06, 0.9999999999999999]$ to obtain results we believe to be correct to, say, at least 20 significant figures. We note that for $c = 0.06$ the value of ν_0 is al-

ready equal to unity to 14 significant figures, and so we did not pursue modifications to our three-line code that could be required for smaller values of c . In addition, we would like to point out that Eqs. (2) are valid also for reactor physics cases where we can have $c > 1$.

Finally, we note that we found

$$\nu_0 = 18.26472572652667373356$$

for the case of $c = 0.999$, and so we believe the result quoted in Ref. 1 is correct to only three or four significant figures and not to the eight figures listed.

III. MAPLE CODE

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f:=(c,x) → arctan(c*Pi*x,2*(1-c*x*arctanh(x)));
y1:=(c) → evalf(exp(-evalf(Int(f(c,x)/x,x=0..1,28))/Pi)/
sqrt(1-c),28);
y2:=(c) → evalf(sqrt((3-2*c)/(3-3*c)-2*evalf(Int(x*f
(c,x),x=0..1,28))/Pi),28);
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C. E. Siewert

North Carolina State University
Mathematics Department
Raleigh, North Carolina 27695-8205

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REFERENCES

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